# Oceania MathsJam Gathering 2022

Combinatorics in Rubik's Cube

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# **OPEN MIC**

Introduction

# MY FAVOURITE MOVIE



## WHAT'S THE MEANING OF LIFE?



## MY FAVOURITE NUMBER



#### COMBINATIONS

43
Quintillion (x 10<sup>30</sup>)

# **RUBIK'S CUBE**

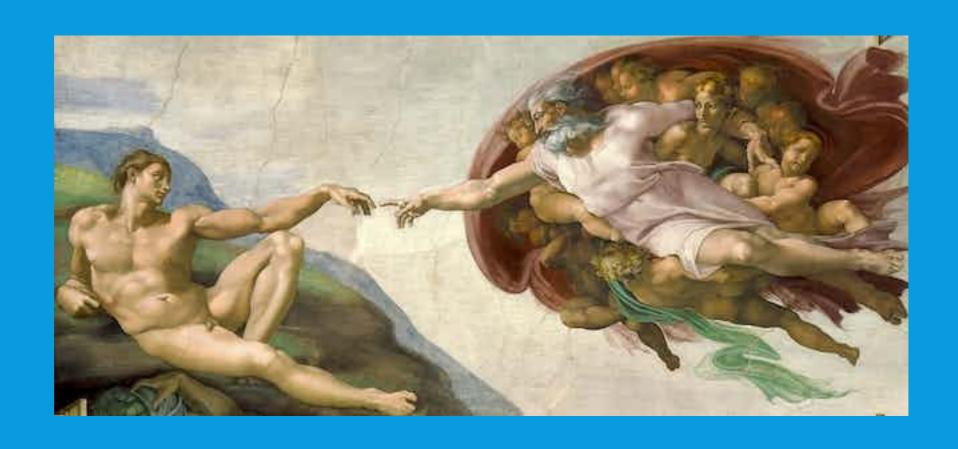


#### TOTAL COMBINATIONS

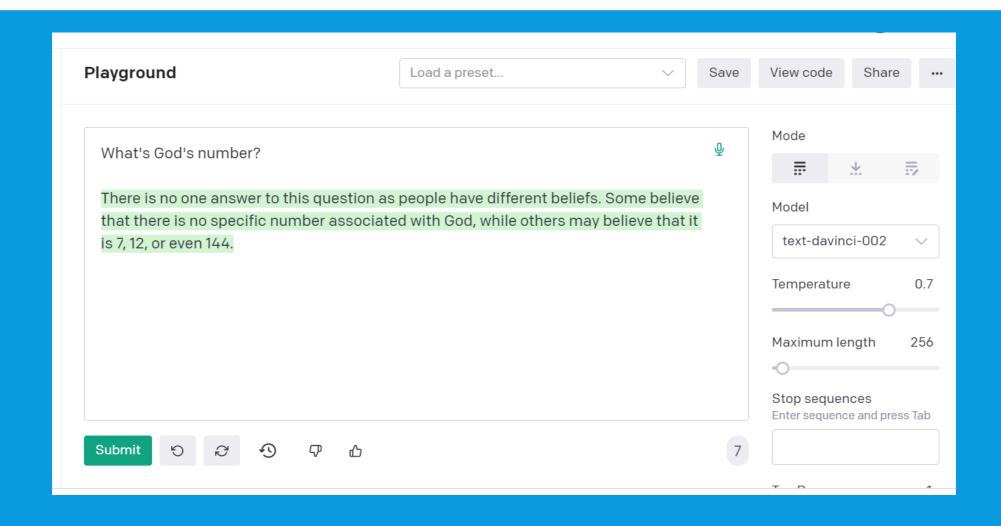
```
12 \times X \times 3^{7}X
! 8! 2^{11} 1/2
= 43 \times 10^{30}
```

# WHAT'S THE MAXIMUM NUMBER OF MOVES A RUBIK'S CUBE CAN BE SOLVED?

# WHAT'S GOD'S NUMBER?



#### OPEN AI - PLAYGROUND



Date	Lower bound	Upper bound	Gap	Notes and Links
July, 1981	18	52	34	Morwen Thistlethwaite proves <u>52 moves</u> suffice.
December, 1990	18	42	24	Hans Kloosterman improves this to <u>42 moves.</u>
May, 1992	18	39	21	Michael Reid shows <u>39 moves</u> is always sufficient.
May, 1992	18	37	19	Dik Winter lowers this to 37 moves just one day later!
January, 1995	18	29	11	Michael Reid cuts the upper bound to <u>29 moves</u> by analyzing <u>Kociemba's two-phase algorithm</u> .
January, 1995	20	29	9	Michael Reid proves that the "superflip" position (corners correct, edges placed but flipped) requires 20 moves.
December, 2005	20	28	8	Silviu Radu shows that <u>28 moves</u> is always enough.
April, 2006	20	27	7	Silviu Radu improves his bound to <u>27 moves</u> .
May, 2007	20	26	6	Dan Kunkle and Gene Cooperman prove <u>26 moves</u> suffice.
March, 2008	20	25	5	Tomas Rokicki cuts the upper bound to <u>25 moves</u> .
April, 2008	20	23	3	Tomas Rokicki and John Welborn reduce it to only <u>23 moves</u> .
August, 2008	20	22	2	Tomas Rokicki and John Welborn continue down to <u>22 moves</u> .
July, 2010	20	20	0	Tomas Rokicki, Herbert Kociemba, Morley Davidson, and John Dethridge prove that God's Number for the Cube is exactly 20.

#### WHAT'S THE MEANING OF LIFE?

4220